Graduate Syllabus MTH621M/D

| Topic/Subtopic  | Learning Strategies/ Activities  | Week/Meeting |
|---|--|--------------|
| <ul><li>1.4 Least Common Multiple</li><li>1.5 Prime and Composite Numbers</li><li>1.6 Unique Factorization</li></ul>  |  |              |
| 2. The Theory of Congruences 2.1 Basic Properties of Congruences 2.2 Linear Congruences 2.3 Linear Diophantine Equations 2.4 The Chinese Remainder Theorem 2.5 Fermat's Theorem 2.6 Wilson's Theorem 2.7 Euler's Phi Function and Its Properties 2.8 Euler's Generalization of Fermat's Theorem | Lecture Facilitated group discussion Problem solving Problem Set                                   | Weeks 3-5    |
| LONG TEST 1   |  | Weeks 6      |
| 3. Primitive Roots 3.1 Exponents and Orders 3.2 Primitive Roots of Prime and Composite Numbers  | Lecture Facilitated group discussion Problem solving Individual Inquiry                            | Weeks 7-8    |
| <ul> <li>4. Quadratic Reciprocity</li> <li>4.1 Euler's Criterion</li> <li>4.2 The Legendre Symbol and Its Properties</li> <li>4.3 Quadratic Residues</li> <li>4.4 The Quadratic Reciprocity Law</li> </ul>  | Lecture Facilitated group discussion Problem solving Problem set                                   | Weeks 9-10   |
| 5. Number Theoretic Functions 5.1 The Functions and 5.2 The Mobius Inversion Formula 5.3 The Greatest Integer Function 5.4 Pythagorean Triples  | Lecture-Discussions Individual/Group ReportingLecture Facilitated group discussion Problem solving | Weeks 11     |
| LONG TEST 2   | Lecture-Discussions<br>Individual/Group Reporting  | Weeks 12     |
| Oral Report: Exposition of Paper  |  | Week 13      |
| FINAL EXAMINATION   |  | Week 14      |

## COURSE REQUIREMENTS

- 2 Long Tests2 Problem Sets
- 1 Final Examination
- 1 Partial exposition of an article on Number Theory

## **SOURCES**

2 laruivivar/2014 Graduate Syllabus MTH621M/D

## **TEXTBOOKS**

• BaD

3 laruivivar/2014